



$$F(a, b) = \frac{1}{\sqrt{a}} \int_{-\infty}^{+\infty} f(t) \psi^* \left(\frac{t-b}{a} \right) dt$$

Wavelets Transform Classifications

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Objective

- talk about briefly the classifications of wavelet transforms

1. Classes of Wavelet Transforms

- divided into two broad classes:
 - continuous wavelet transforms
 - discrete wavelet transforms

(1) Continuous Wavelet Transforms (CWT)

- continuous scale parameter(a) and shift (position) parameter (b)

$$C(a, b) = \int_{-\infty}^{\infty} f(t) \psi_{a,b}^*(t) dt$$

where: the * is the complex conjugate symbol, $a \in \mathbb{R}^{+*}$, $b \in \mathbb{R}$

- Base wavelet:

$$\psi_{a,b}(t) = \frac{1}{\sqrt{a}} \psi \left(\frac{t-b}{a} \right)$$

By continuously varying the values of the scale parameter, a , and the position parameter, b , we obtain the cwt coefficients $C(a, b)$.

(2) Discrete Wavelet Transforms

- Any wavelet transforms for which the wavelets are discretely sampled
- the sampling of the frequency axis corresponds to dyadic sampling
- the scale parameter is discretized to integer powers of 2
- Base wavelet:

$$\psi_{s,\tau}(t) = \frac{1}{\sqrt{2^j}} \psi\left(\frac{t - 2^j k}{2^j}\right)$$

$$\text{where: } a = 2^j, b = 2^j k$$

As the signal $f(t)$ occurs at discrete integer time steps t , the dyadic discrete wavelet transforms can be written as:

$$C(j, k) = \frac{1}{\sqrt{2^j}} \sum_{j,k \in \mathbb{Z}} f(t) \psi_{(2^j, 2^j k)}$$

- The discrete wavelet transforms (DWT) decomposes a signal into a set of mutually orthogonal wavelet basis functions.

2. Other Classification Methods

- Data Dimensions
 - 1D
 - 2D
 - nD
- Decomposition Levels
 - single level
 - multilevel
- Discrete Wavelet Transforms
 - Discrete Wavelet Transform (DWT)
 - Stationary Wavelet Transform (SWT)
 - Multiresolution Analysis (MRA)
 - Wavelet Packet Transform (WPT)
 - Maximum Overlap Discrete Wavelet Transform (MODWT)
 - Multiresolution Analysis based on MODWT (MODWTMRA)